

1. Why must budget constraints be binding?
 - A. We do not model savings so we would never save
 - B. We maximize utility and more goods bought = more utility**
 - C. Money has no value
 - D. Money loses value so it will be worth less tomorrow

2. Find the utility maximizing amount of each good for the following utility functions subject to budgets $M = P_x X + P_y Y$:
 - (a) $U(x, y) = x^{1/2}y^{1/2}$ s.t. $120 = 4x + y$
 - (b) $U(x, y) = \alpha \ln(x) + y$ s.t. $M = P_x x + P_y y$
 - (c) $U(x, y) = \min\{2x, y\}$ s.t. $16 = 2x + y$
 - (d) $U(x, y) = 4x + 5y$ s.t. $10 = 2x + 3y$

Solution:

$$(a) \ x^* = \frac{1}{2} \cdot \frac{120}{4} = 15 \quad \& \quad y^* = \frac{1}{2} \cdot \frac{120}{1} = 60$$

$$(b) \ x^* = \frac{\alpha}{x} = \frac{4}{1} \rightarrow 4x = \alpha \rightarrow x^* = \frac{\alpha}{4} \quad \& \quad 120 = 4\left(\frac{\alpha}{4}\right) + y \rightarrow y^* = 120 - \alpha$$

$$(c) \ 2x = y \rightarrow 16 = 2 \cdot x + 2x \rightarrow x^* = 4 \quad \& \quad y^* = 2(4) = 8$$

$$(d) \ MRS = \frac{P_x}{P_y} \rightarrow \frac{4}{5} = \frac{2}{3} \rightarrow MRS > Price\ Ratio \rightarrow y^* = 0 \rightarrow x^* = 5$$

3. Draw a utility maximizing Indifference Curve subject to an arbitrary budget for the following function types:
 - (a) Cobb-Douglas
 - (b) Quasi-linear
 - (c) Perfect Complements
 - (d) Perfect Substitutes (Show both possible corner solutions)

